

Buddhist and Jain Logic.
Forerunners of Modern Paraconsistent Logic?

Graham Priest

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First Degree Entailment

Jainism and the Saptabhaṅgī

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Buddhist and Jain Logic: Forerunners of Modern Paraconsistency?

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■ Explosion: $A, \neg A \vdash B$

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- Explosion: $A, \neg A \vdash B$
- A consequence relation is *paraconsistent* if Explosion is *not* valid.

Syllogistic

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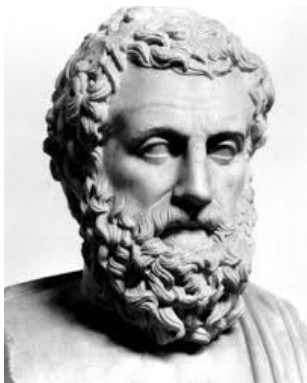
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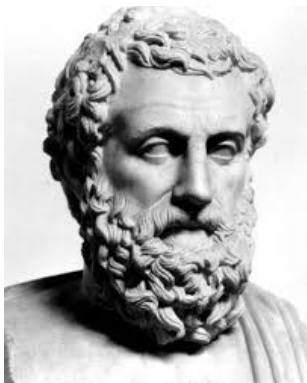
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No *As* are *Bs*
Some *Bs* are *As*
So all *As* are *As*

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“How is it, Master Gotama, does Master Gotama hold the view: ‘After death a Tathāgata exists: only this is true, anything else is wrong’?”

“Vaccha, I do not hold the view: ‘After death a Tathāgata exists: only this is true, anything else is wrong.’”

“How then, does Master Gotama hold the view: ‘After death a Tathāgata does not exist: only this is true, anything else is wrong’?”

“Vaccha, I do not hold the view: ‘After death a Tathāgata does not exist: only this is true, anything else is wrong.’”

“How is it, Master Gotama, does Master Gotama hold the view: ‘After death a Tathāgata both exists and does not exist: only this is true, anything else is wrong.’?”

“Vaccha, I do not hold the view: ‘After death a Tathāgata both exists and does not exist: only this is true, anything else is wrong.’ ” “How then, does Master Gotama hold the view: ‘After death a Tathāgata neither exists nor does not exist: only this is true, anything else is wrong’?”

“Vaccha, I do not hold the view: ‘After death a Tathagata neither exists nor does not exist: only this is true, anything else is wrong.’”

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- Truth values:
 - t (just true)
 - f (just false)
 - b (both)
 - n (neither)

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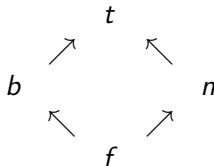
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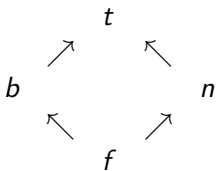
Conclusion

- Truth values:
 - t (just true)
 - f (just false)
 - b (both)
 - n (neither)



Conjunction and Disjunction

- $A \wedge B$ is true if A is true and B is true



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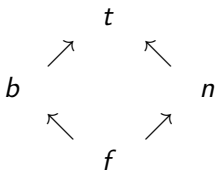
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- $A \wedge B$ is true if A is true and B is true
- $A \wedge B$ is false if A is false or B is false



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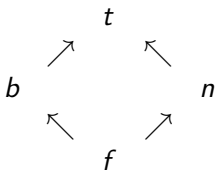
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- $A \wedge B$ is true if A is true and B is true
- $A \wedge B$ is false if A is false or B is false
- If A is t and B is b , $A \wedge B$ is b



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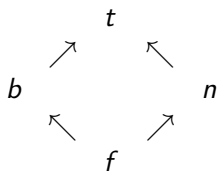
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- $A \wedge B$ is true if A is true and B is true
- $A \wedge B$ is false if A is false or B is false

- If A is t and B is b , $A \wedge B$ is b
- If A is b and B is n , $A \wedge B$ is n

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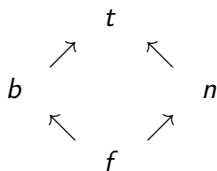
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- $A \wedge B$ is true if A is true and B is true
- $A \wedge B$ is false if A is false or B is false
- If A is t and B is b , $A \wedge B$ is b
- If A is b and B is n , $A \wedge B$ is n
- The value of $A \wedge B$ is the *glb* of the values of A and B

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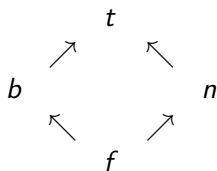
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- $A \wedge B$ is true if A is true and B is true
- $A \wedge B$ is false if A is false or B is false

- If A is t and B is b , $A \wedge B$ is b
- If A is b and B is n , $A \wedge B$ is n

- The value of $A \wedge B$ is the *glb* of the values of A and B
- The value of $A \vee B$ is the *lub* of the values of A and B

Negation

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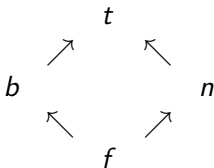
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- $\neg A$ is true if A is false
- $\neg A$ is false if A is true



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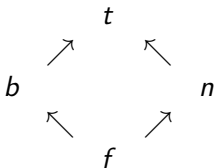
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- $\neg A$ is true if A is false
- $\neg A$ is false if A is true
- If A is t , $\neg A$ is f ; and vice versa

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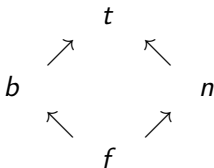
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- $\neg A$ is true if A is false
- $\neg A$ is false if A is true
- If A is t , $\neg A$ is f ; and vice versa
- If A is b , $\neg A$ is b .

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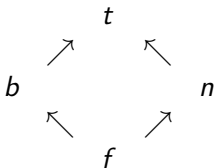
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- $\neg A$ is true if A is false
- $\neg A$ is false if A is true
- If A is t , $\neg A$ is f ; and vice versa
- If A is b , $\neg A$ is b .
- If A is n , $\neg A$ is n .

Validity

- An inference is valid if whenever the premises are true (i.e., t or b) so is the conclusion.

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Conclusion

- An inference is valid if whenever the premises are true (i.e., t or b) so is the conclusion.

- $\neg\neg A \models A$

- $A \models \neg\neg A$

Validity

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Conclusion

- An inference is valid if whenever the premises are true (i.e., t or b) so is the conclusion.
- $\neg\neg A \models A$
- $A \models \neg\neg A$
- $A, \neg A \not\models B$

Validity

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- An inference is valid if whenever the premises are true (i.e., t or b) so is the conclusion.

- $\neg\neg A \models A$

- $A \models \neg\neg A$

- $A, \neg A \not\models B$

- A is b , B is f

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■ *Anekāntavāda*

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- *Anekāntavāda*
- *Syāt*

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- *Anekāntavāda*
- *Syāt*
- Truth values:
 - *t* (just true)
 - *f* (just false)
 - *i* (?)

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- *Anekāntavāda*
- *Syāt*
- Truth values:
 - *t* (just true)
 - *f* (just false)
 - *i* (?)
- $2^3 - 1 = 7$

The Saptabhaṅgī

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The seven predicate theory consists in the use of seven claims about sentences, each preceded by 'arguably' or 'conditionally' (syāt) [all] concerning a single object and its particular properties, composed of assertions and denials, either simultaneously or successively, and without contradiction. They are as follows:

(1) Arguably, it (i.e., some object) exists. The first predicate pertains to an assertion.

(2) Arguably, it does not exist. The second predicate pertains to a denial.

(3) Arguably, it exists; arguably it does not exist. The third predicate pertains to successive assertion and denial.

(4) Arguably, it is non-assertable. The fourth predicate pertains to a simultaneous assertion and denial.

(5) Arguably, it exists; arguably it is non-assertable. The fifth predicate pertains to an assertion and a simultaneous assertion and denial.

(6) Arguably, it does not exist; arguably it is non-assertable. The sixth predicate pertains to a denial and a simultaneous assertion and denial.

(7) Arguably, it exists; arguably it doesn't exist; arguably it is non-assertable. The seventh predicate pertains to a successive assertion and denial and a simultaneous assertion and denial.

Vādideva Sūri (c. 12th Century)

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K_3 and LP

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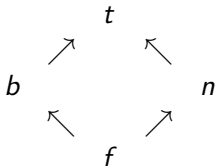
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K_3 and LP

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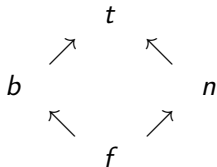
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$$\begin{array}{c} t \\ \uparrow \\ b \\ \uparrow \\ f \end{array} = i = \begin{array}{c} t \\ \uparrow \\ n \\ \uparrow \\ f \end{array}$$

Conjunction and Disjunction

- To compute the values of $A \wedge B$, you combine all the values of A and B

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Conjunction and Disjunction

- To compute the values of $A \wedge B$, you combine all the values of A and B
- Suppose that A has the values t and f , and B has the values t and i

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- To compute the values of $A \wedge B$, you combine all the values of A and B
- Suppose that A has the values t and f , and B has the values t and i

\wedge	t	i
t	t	i
f	f	f

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Conjunction and Disjunction

- To compute the values of $A \wedge B$, you combine all the values of A and B
- Suppose that A has the values t and f , and B has the values t and i

\wedge	t	i
t	t	i
f	f	f

- $A \wedge B$ has the values, t, i, f .

Conjunction and Disjunction

- To compute the values of $A \wedge B$, you combine all the values of A and B
- Suppose that A has the values t and f , and B has the values t and i

\wedge	t	i
t	t	i
f	f	f

- $A \wedge B$ has the values, t, i, f .
- Similarly for $A \vee B$

Negation

- To compute the values of $\neg A$, you negate all the values for A

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- To compute the values of $\neg A$, you negate all the values for A
- Suppose that A has the values t and i :

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- To compute the values of $\neg A$, you negate all the values for A
- Suppose that A has the values t and i :

A	t	i
$\neg A$	f	i

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- To compute the values of $\neg A$, you negate all the values for A
- Suppose that A has the values t and i :

A	t	i
$\neg A$	f	i

- $\neg A$ has the values f and i .

Validity

- An inference is valid if whenever the premises have the value t or b so does the conclusion.

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Validity

- An inference is valid if whenever the premises have the value t or b so does the conclusion.
- Whatever i is, the logic is paraconsistent

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Jainism and
the
Saptabhaṅgī

Plurivalent
Logic

Conclusion

- An inference is valid if whenever the premises have the value t or b so does the conclusion.
- Whatever i is, the logic is paraconsistent
- Let A have the values t and f .

Validity

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- $A, \neg A \not\equiv B$.

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